Don’t Tell a Mathematician They Can’t Solve an Equation

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Conclusion: The solutions to $x^2 + 1 = 0$ are: $x = \pm\mathrm{i}$

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Example: Find the solutions to:

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We can re-write this in terms of i and not need another new number.

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