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To get it in this form, we need to multiply the top and bottom of the fraction by the conjugate of the bottom.