

Perpendicular and Parallel Lines

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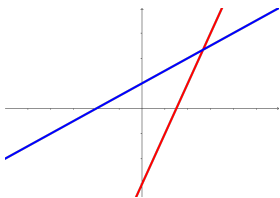
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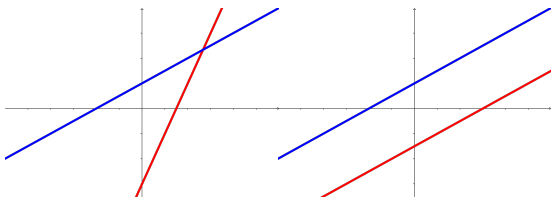
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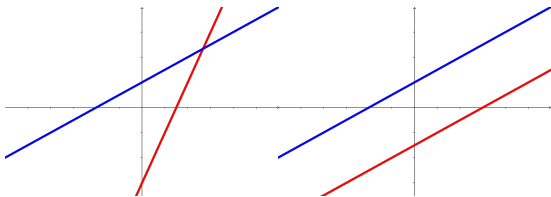
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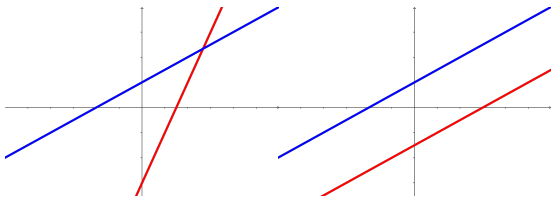
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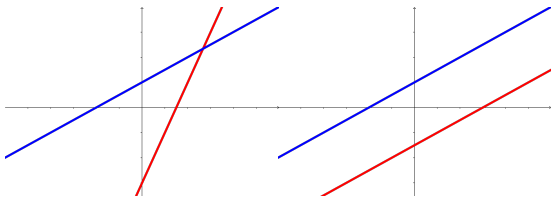
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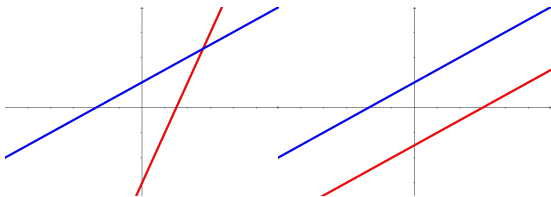
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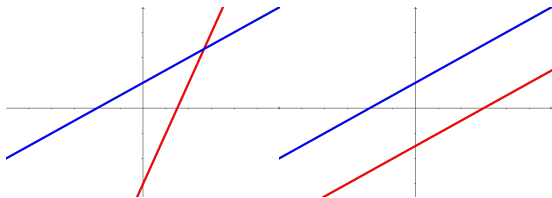
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If two lines have slopes m_1 and m_2 then:

The lines are parallel $\iff m_1 = m_2$

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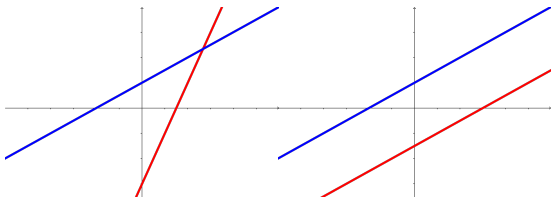
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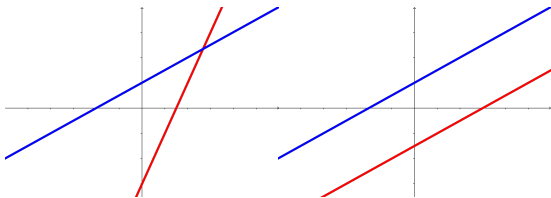


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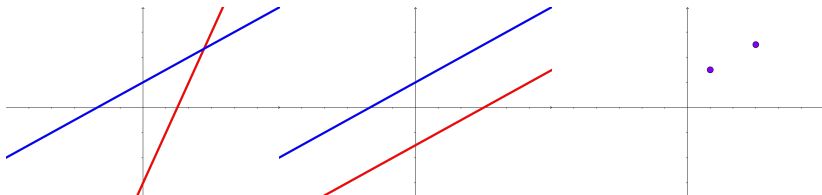
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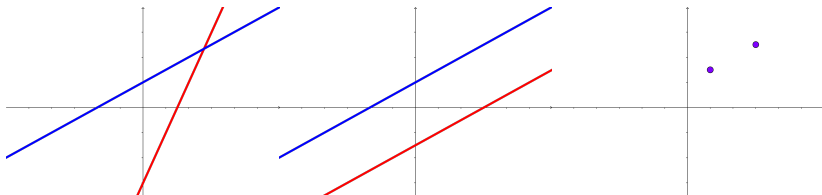
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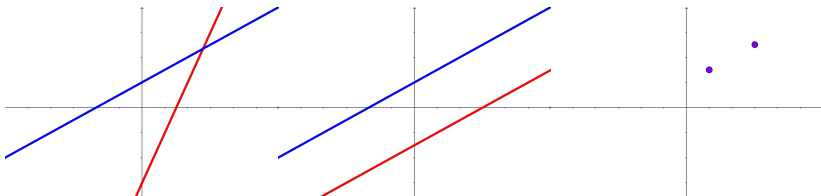
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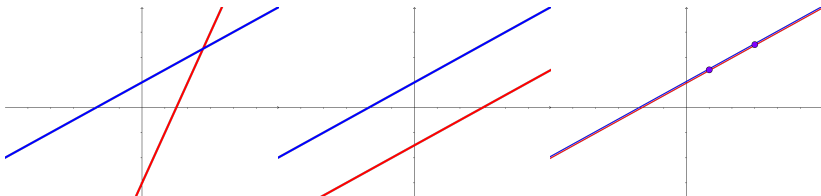
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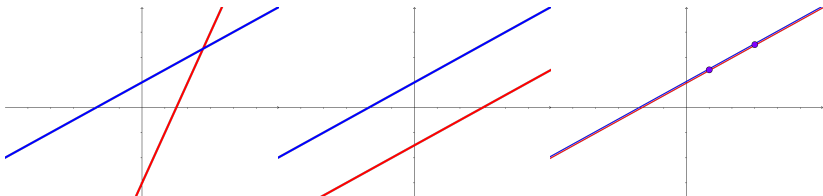
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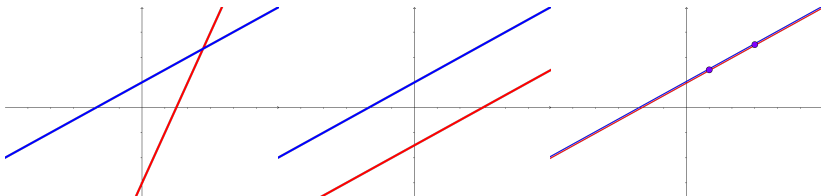
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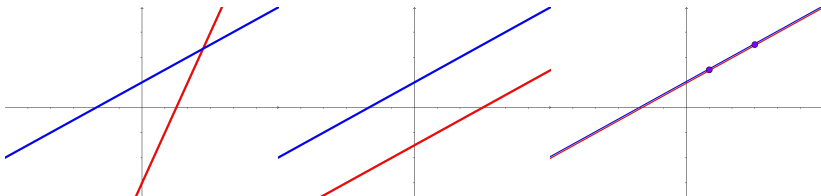
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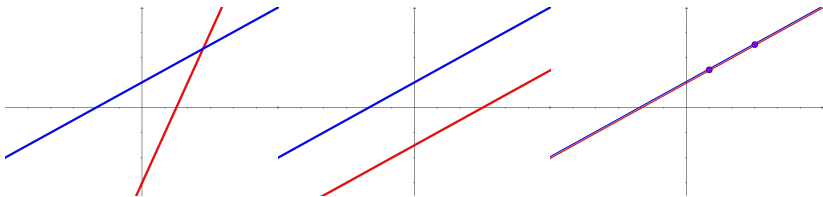
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The two main questions that arise are: Where? How?

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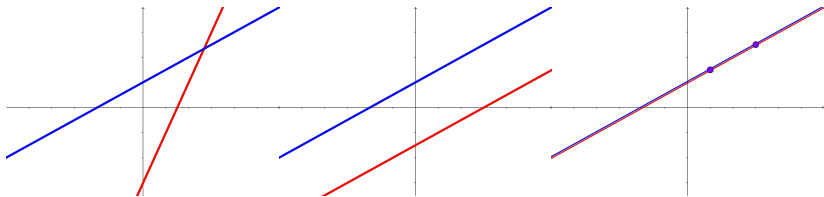
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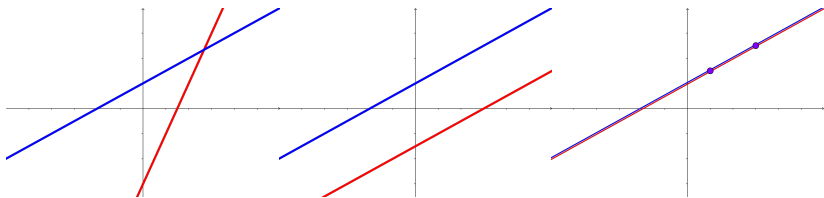
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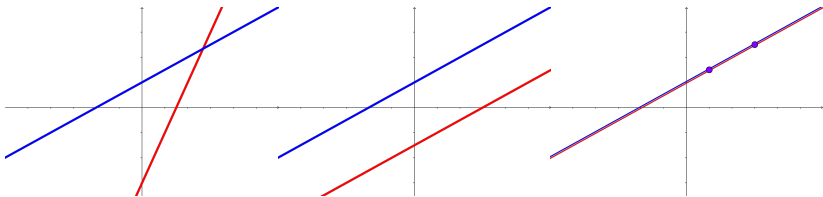
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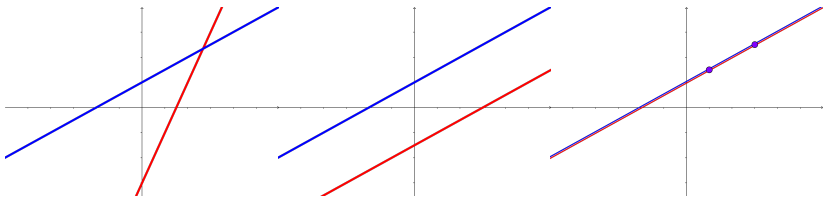
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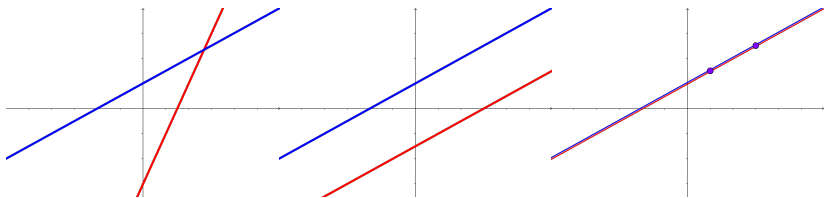
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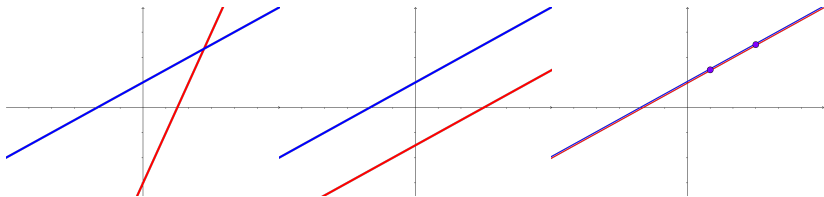
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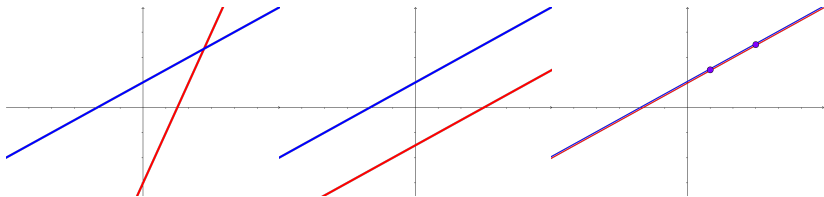
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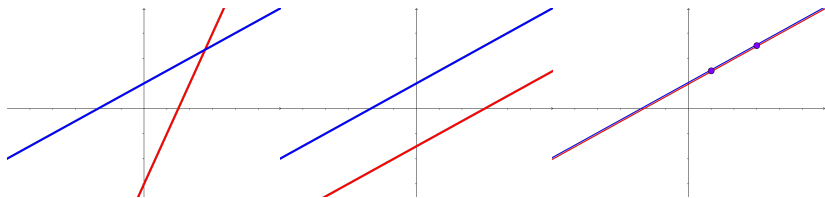
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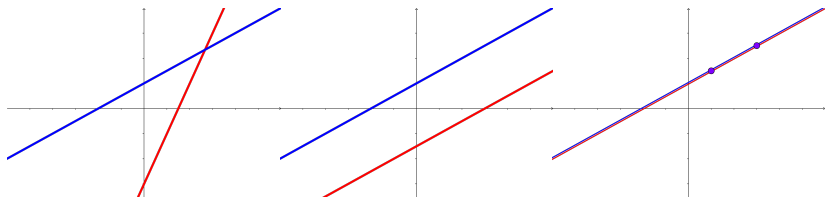
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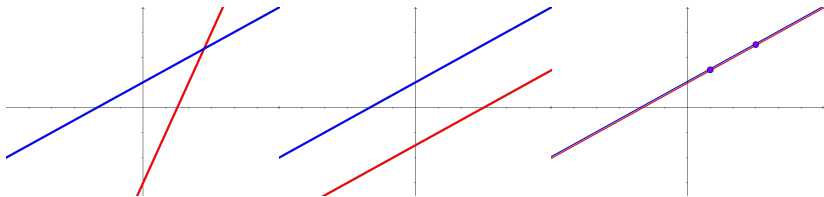


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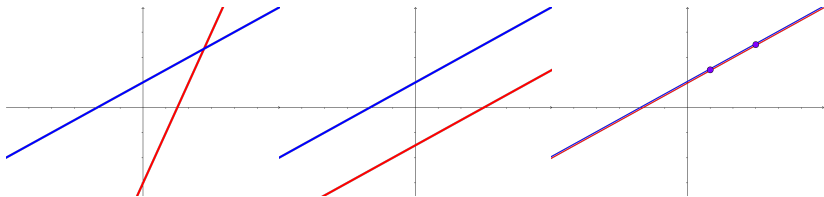
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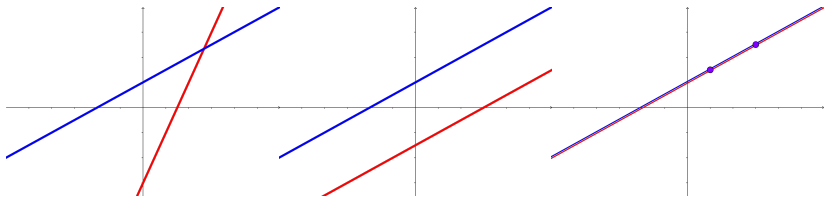


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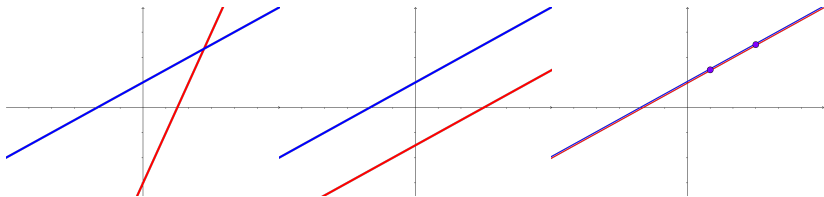
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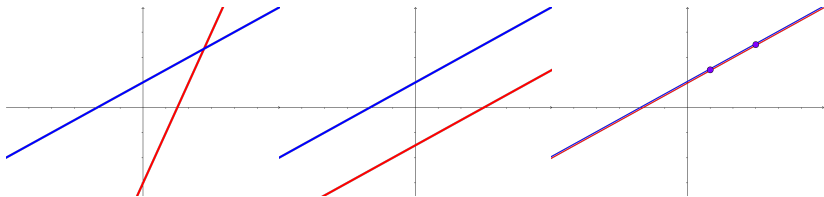
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