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Since our equation is defined at  $x = -8$ , we can conclude:

**Conclusion:** The solution to  $\frac{2}{x+4} = \frac{3}{x+2}$  is  $x = -8$