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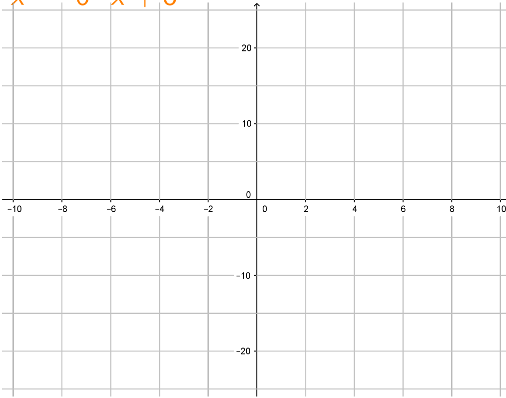

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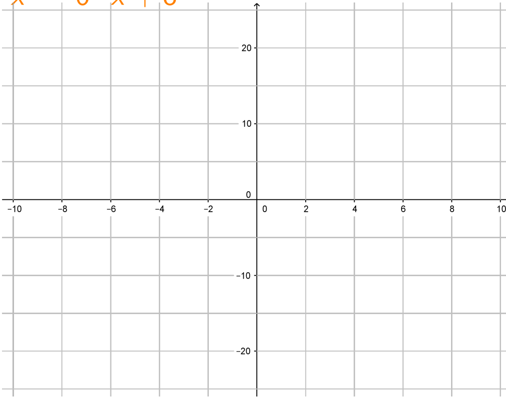

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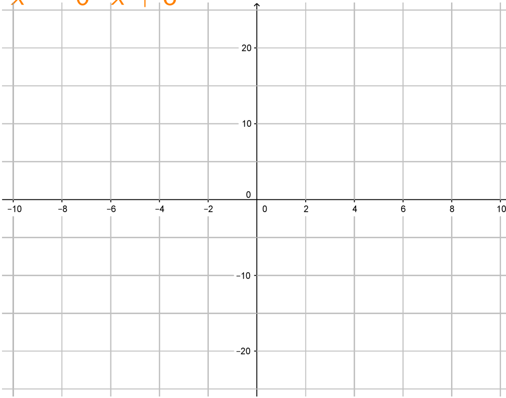

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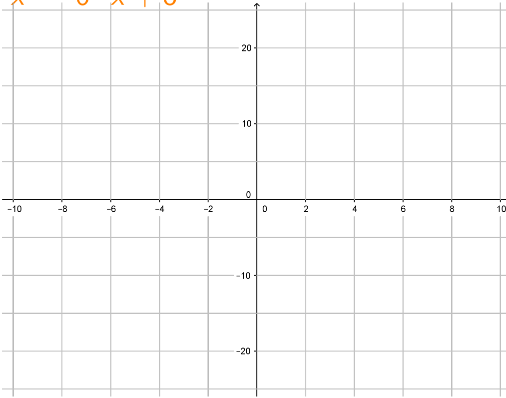

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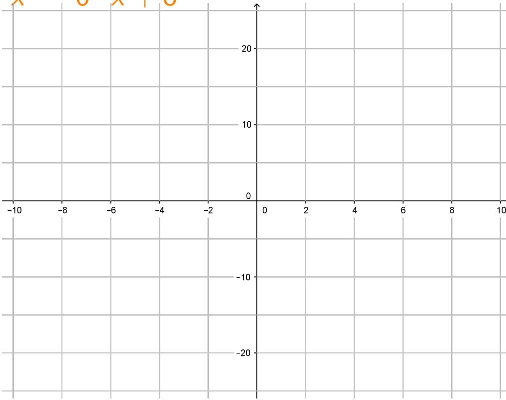

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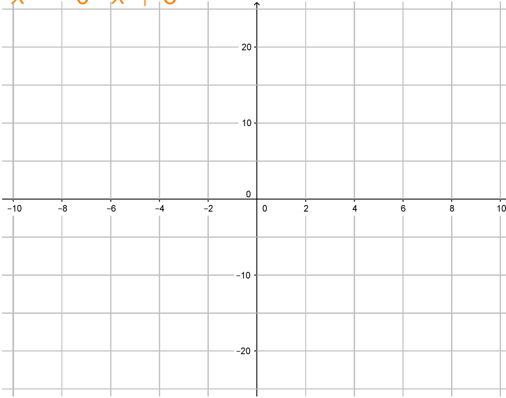

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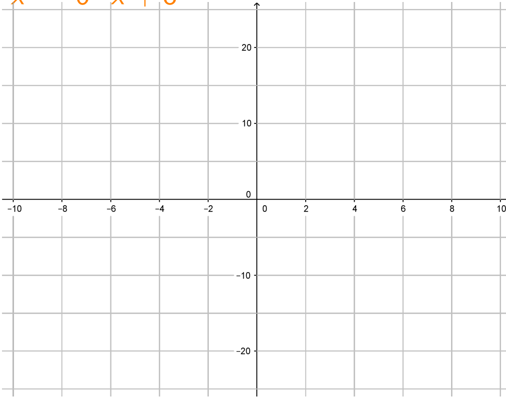

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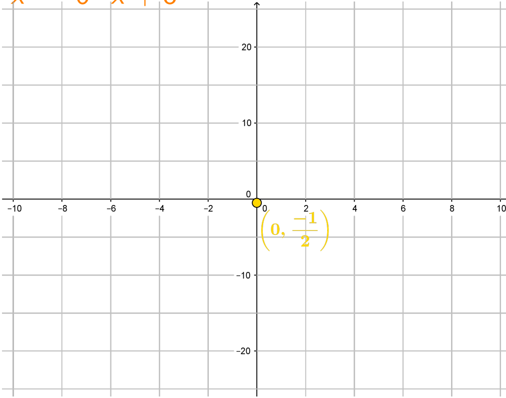

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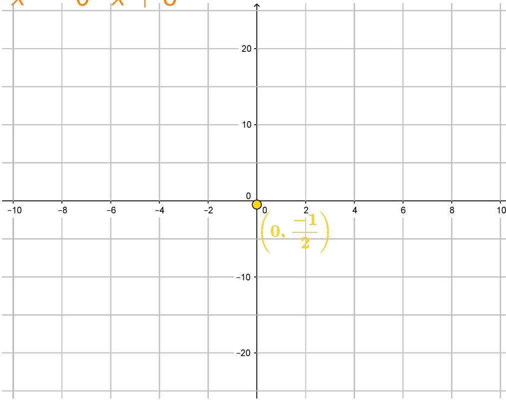

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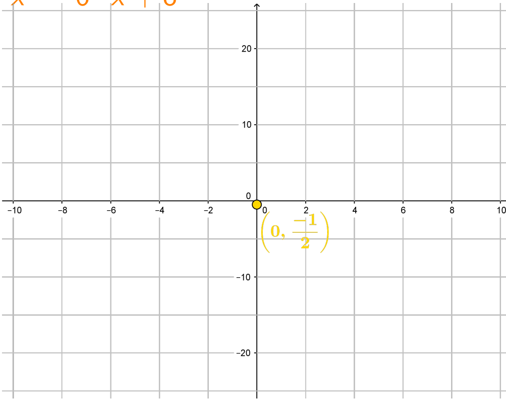

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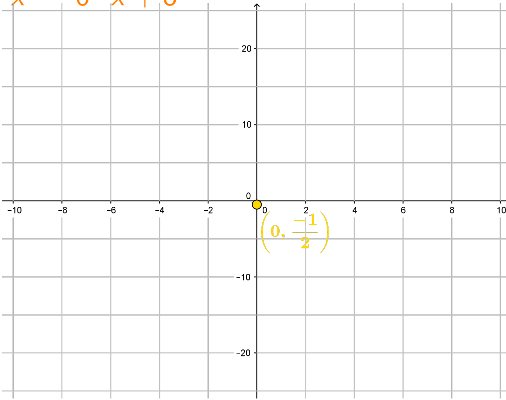

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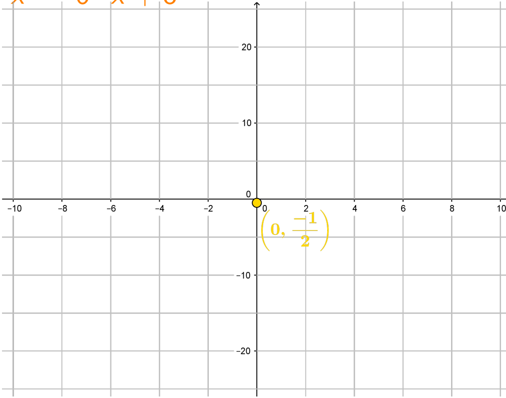

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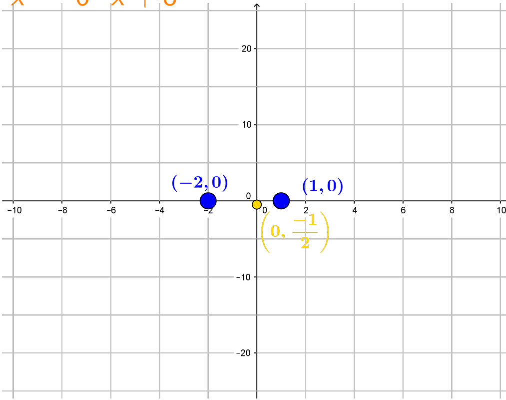

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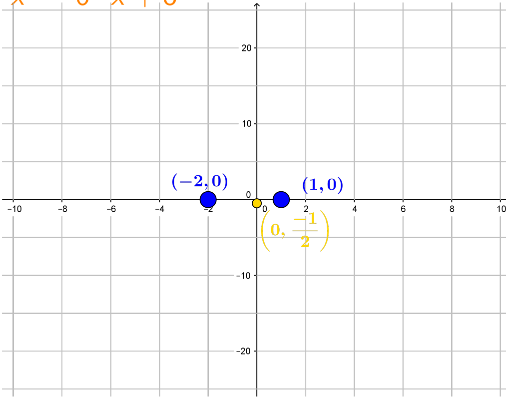

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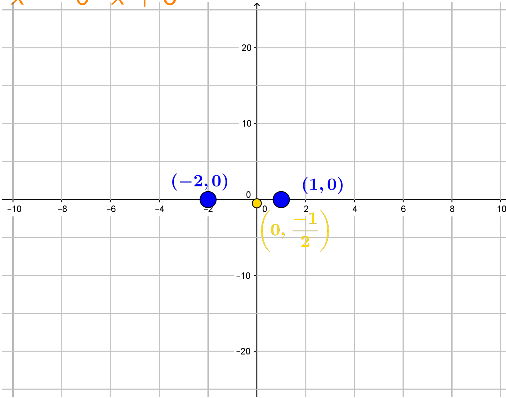

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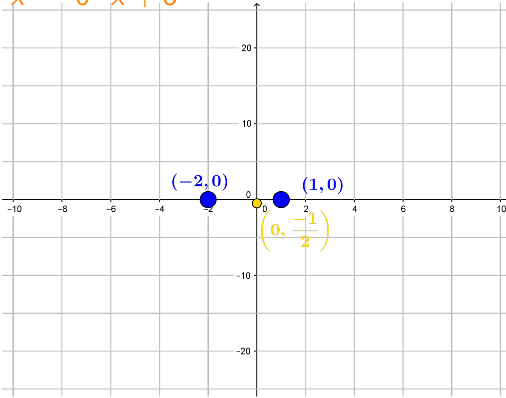

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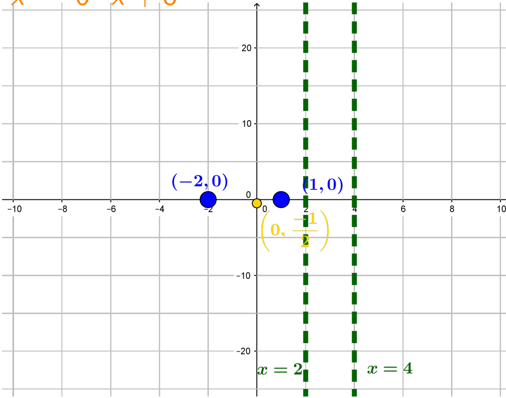

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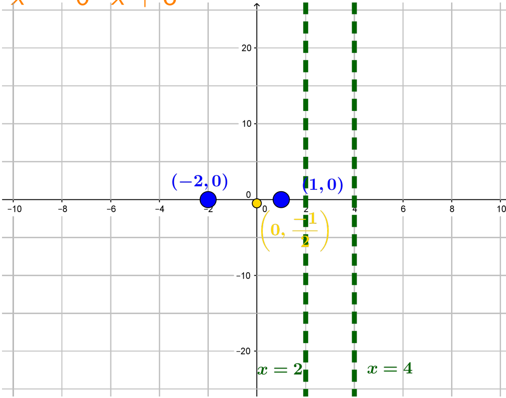

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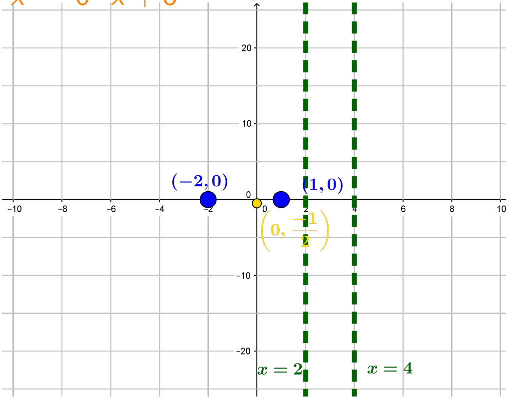

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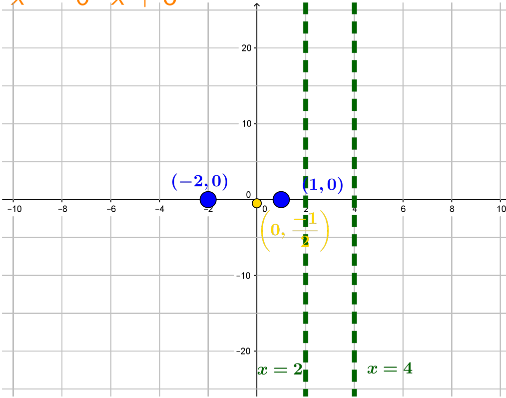

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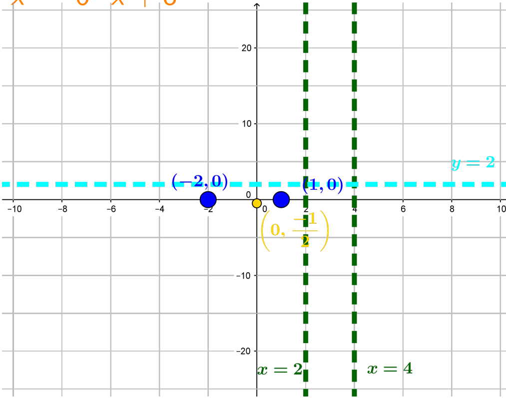

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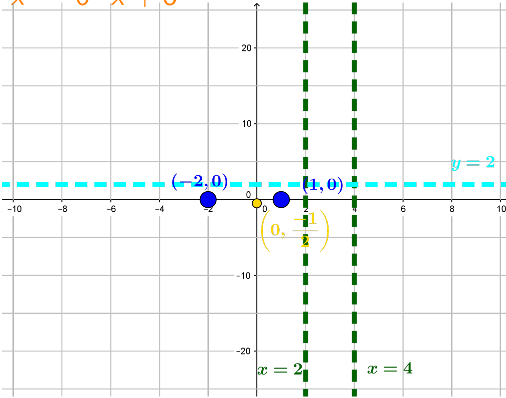

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The End Behavior: $x \to \pm\infty$ Called a *Horizontal Asymptote*

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▸ Like Polynomials we need to check if $f(x) > 0$ or $f(x) < 0$ on some intervals

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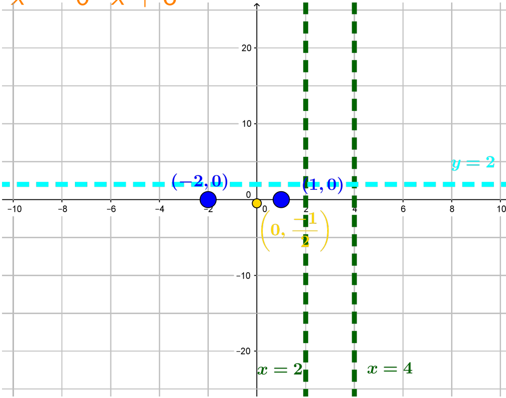

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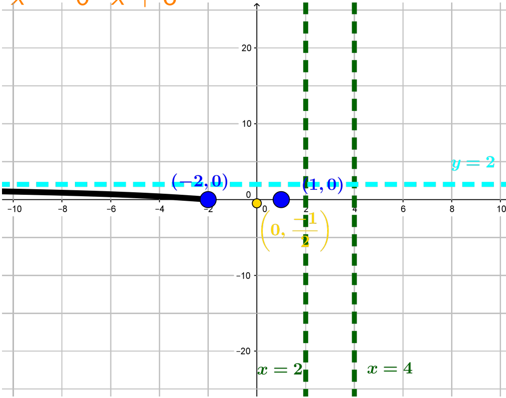

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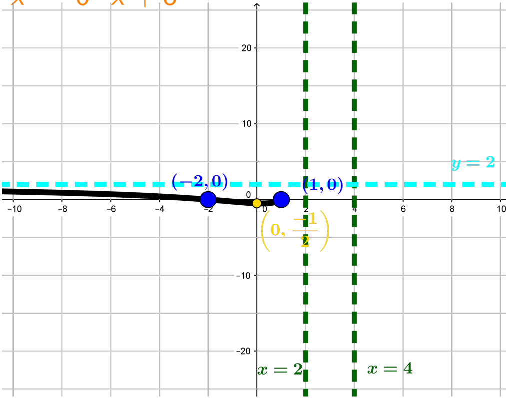

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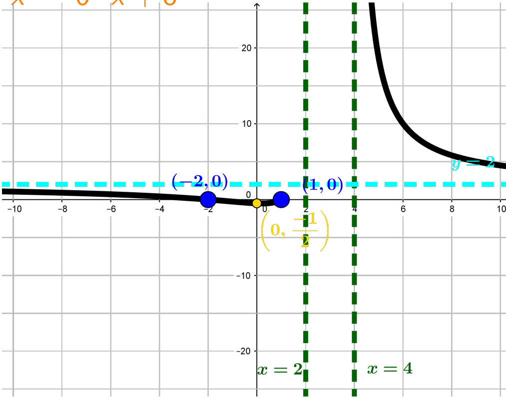

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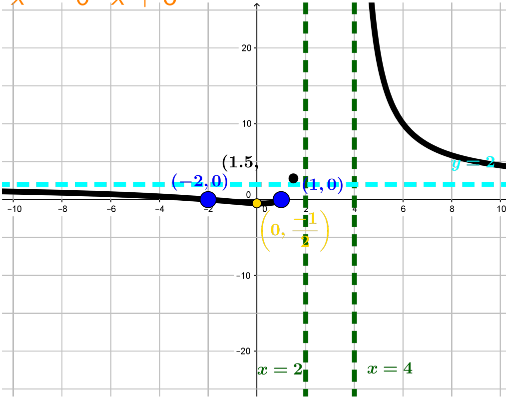

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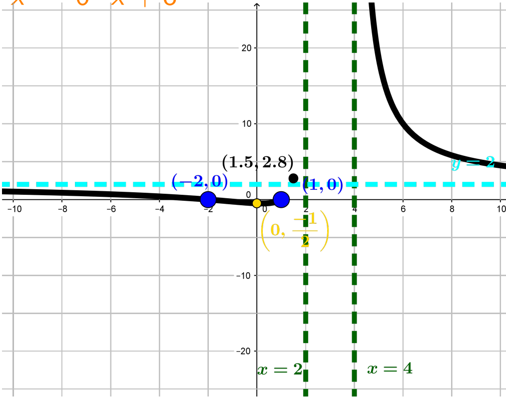

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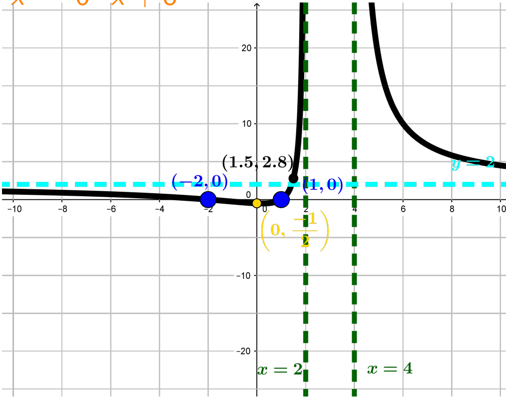

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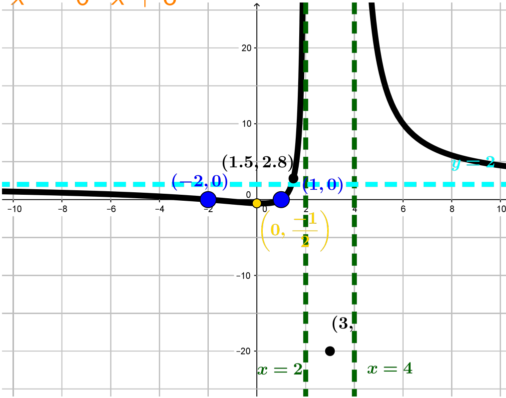

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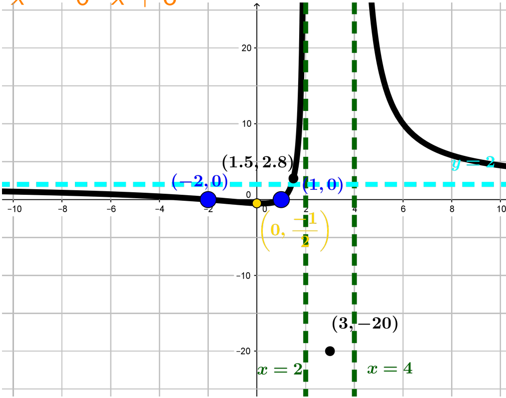

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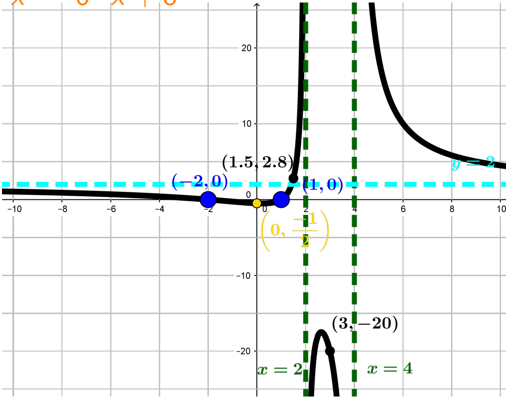

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