

Solving Quadratics without Factoring - Example

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Adding 2 to both sides gives: $x = 2 \pm \sqrt{\frac{11}{3}}$

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Adding 2 to both sides gives: $x = 2 \pm \sqrt{\frac{11}{3}} = 2 + \sqrt{\frac{11}{3}}, 2 - \sqrt{\frac{11}{3}}$