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If we can, then we can use the same method to solve: $x^2 - 5x - 6 = 0$

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If we want these two sides to be the **same** we need

$$-5 = s + t \qquad\qquad -6 = st$$

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Can we pick s and t that make these true?

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The solutions to $0 = x^2 - 5x - 6$ are $x = -1, 6$