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Conclusion: The solution to $2^{(x+1)} = 3^x$ is: $x = \frac{ln(2)}{(ln(3) - ln(2))} \approx 1.7095$