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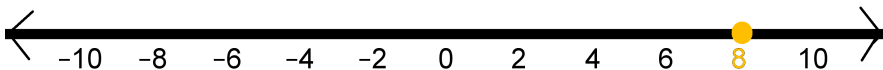
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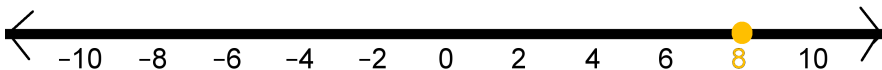
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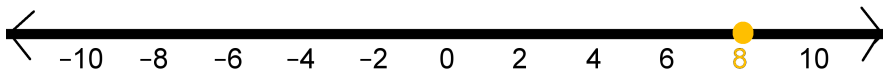
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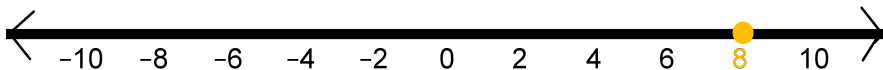
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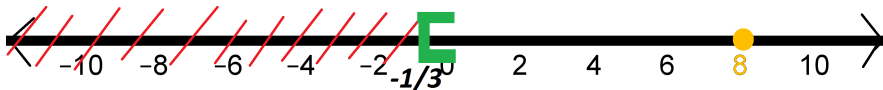
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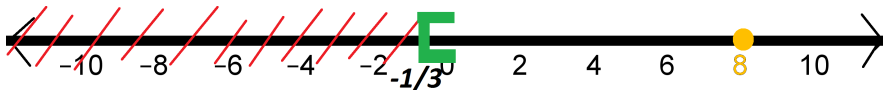
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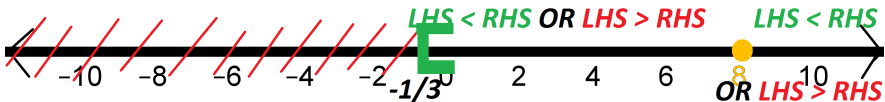
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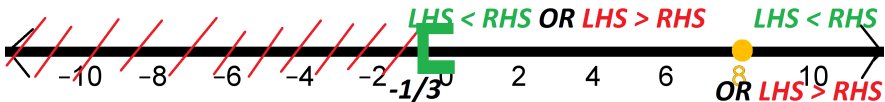
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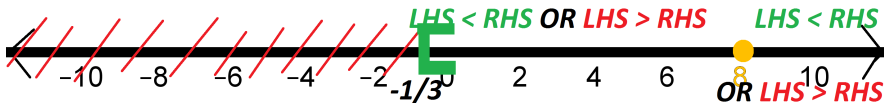
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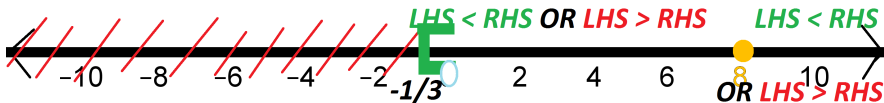
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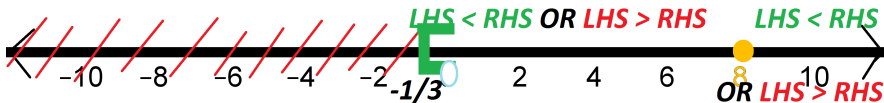
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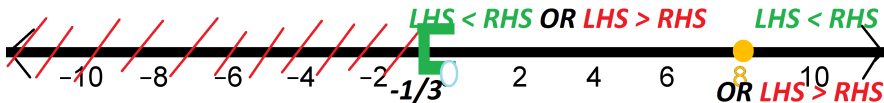
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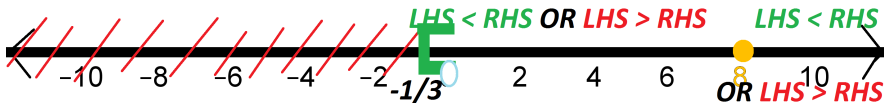
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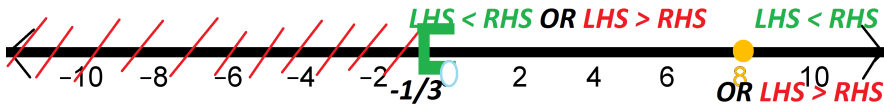
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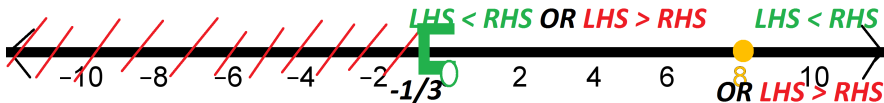
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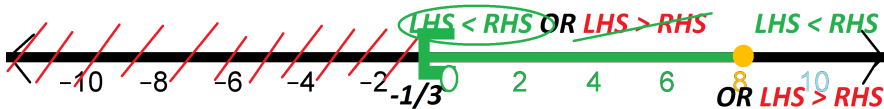
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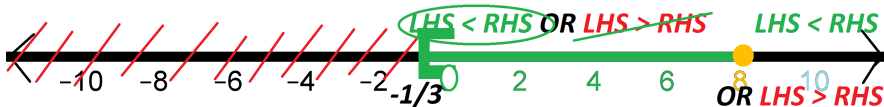
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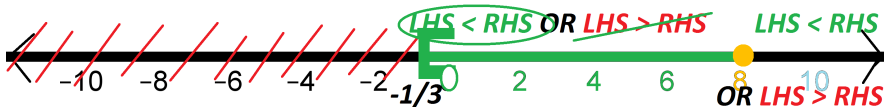
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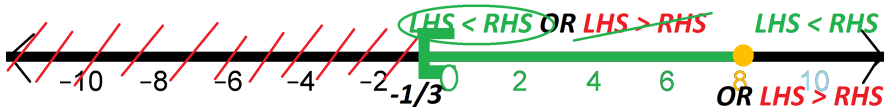
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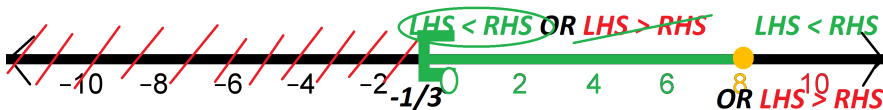
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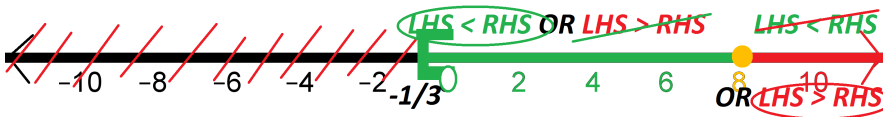
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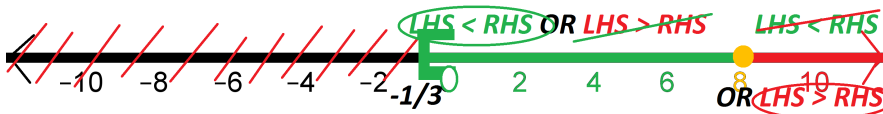
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**Conclusion:** The solutions to  $\sqrt{3x+1} \leq 5$  are:  $\left[\frac{-1}{3}, 8\right]$