

Remainder Theorem and Factoring

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We just see here that it is true for polynomials with higher degrees.