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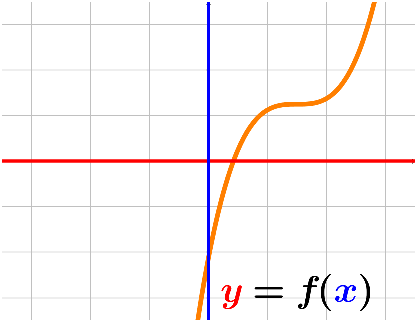

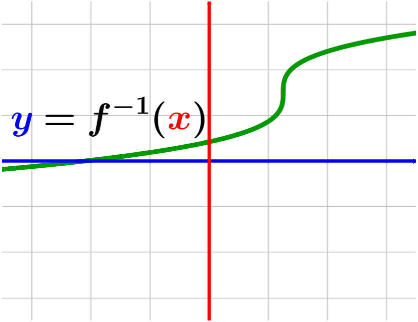

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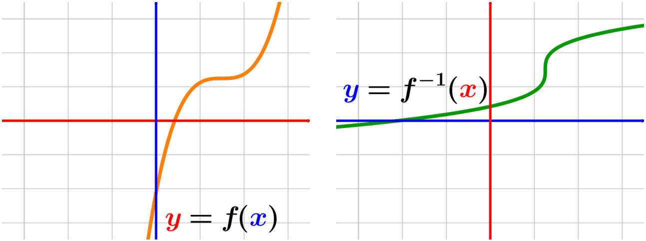

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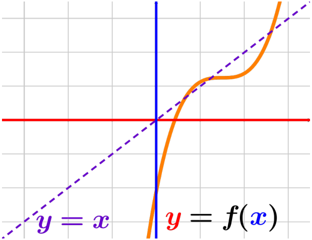
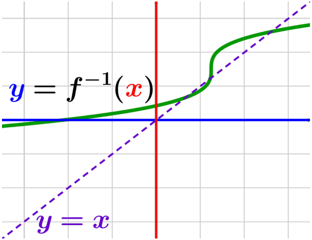
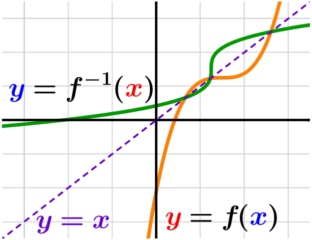




If we graph these on the same plane, we can make the observation that switching the roles of x and y reflects the graph across the line $y = x$



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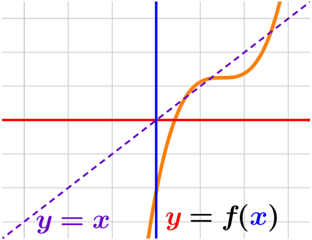

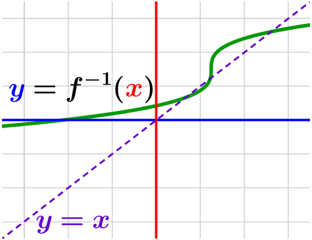

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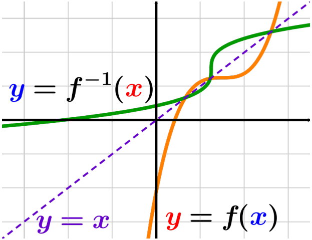

In General: The graph $y = f^{-1}(x)$ is the graph of $y = f(x)$ reflected across the line $y = x$