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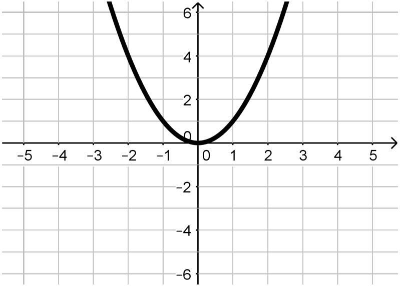

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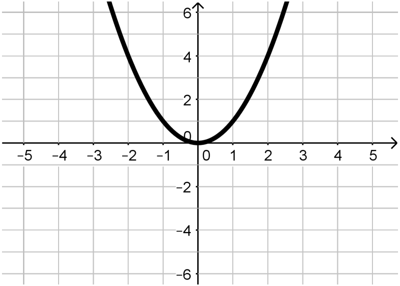

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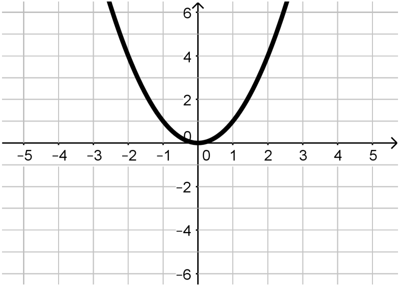

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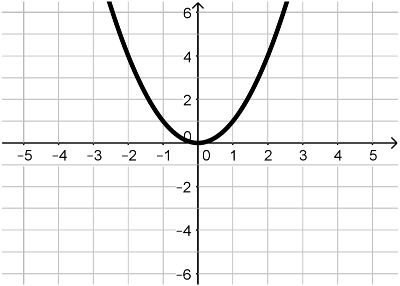

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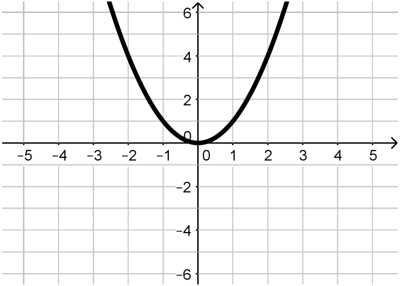

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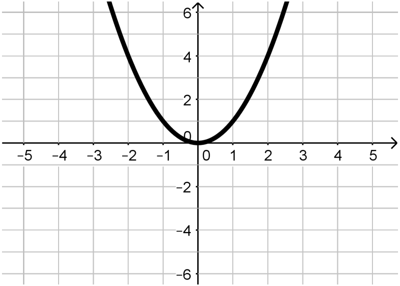

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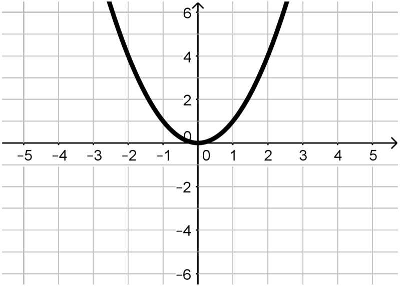

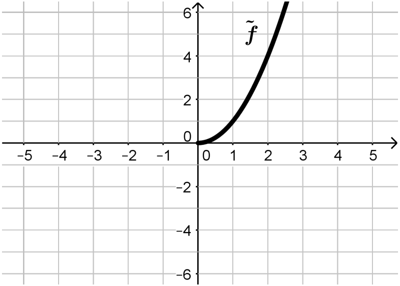

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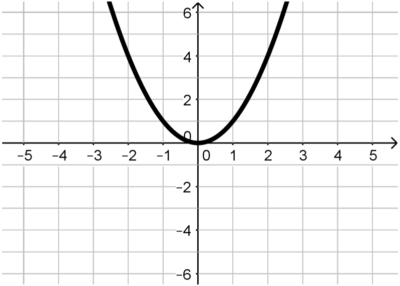

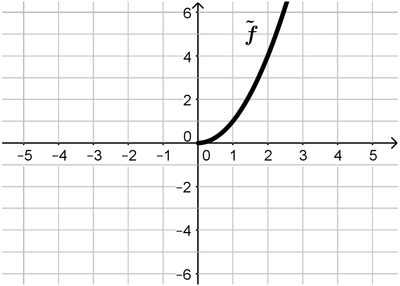

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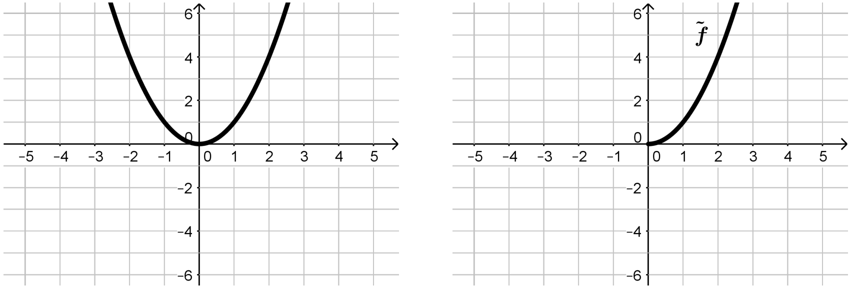

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We have found it before! $\tilde{f}^{-1} = \sqrt{x}$

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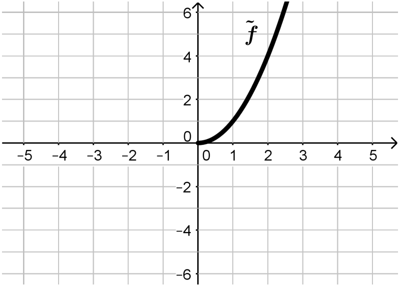

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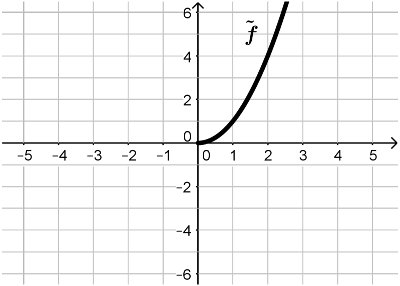

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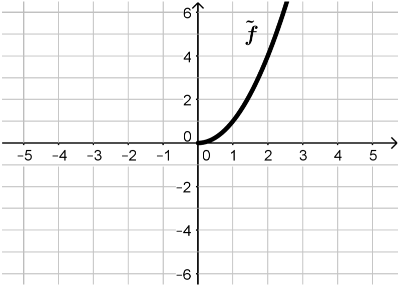

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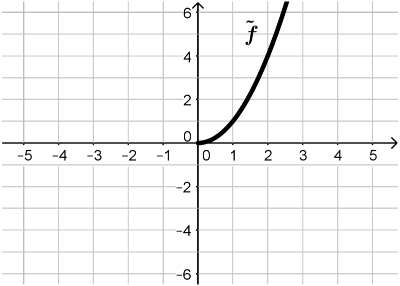

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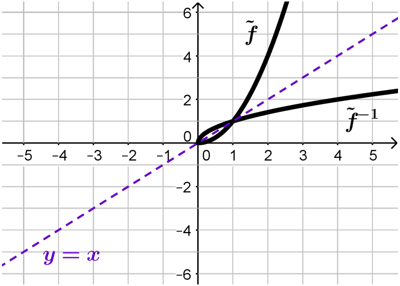

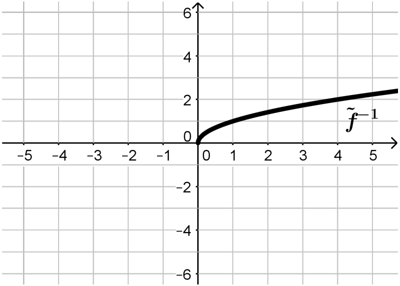

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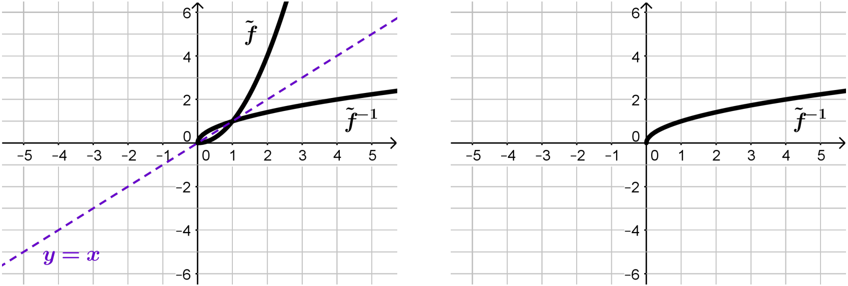

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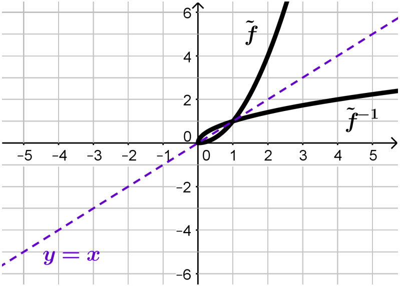

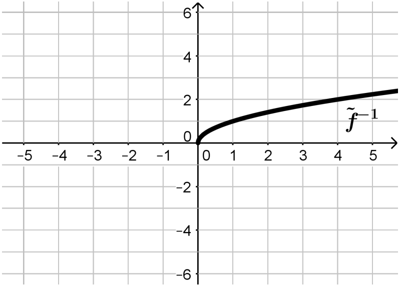

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