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Notice: f^{-1} undoes the actions of f: Multiplying by 2 then Adding 3 by Subtracting 3 then Dividing by 2