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as a function so that $x = f^{-1}(f(x))$ and $x = f(f^{-1}(x))$

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If $y = f(x)$ is a 1-1 function, then $y = f^{-1}(x)$ is the *inverse function* if:

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