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Example: Determine if the function $f(x)$ is even, odd, or neither

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Let's compute $f(-x)$ and see if it is the same as $f(x)$

$f(-x) = (-x)^3 + 1$

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Note: We were able to quickly check if this function was even or odd, without ever needing to draw a graph!