

Distributive Law of Exponents over Multiplication

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$$\begin{aligned}(2x)^3 &= 2^3 x^3 \\ &= 8x^3\end{aligned}$$