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4 + 5 combined allows us to define exponents for all fractions! It is fun to notice that our understanding of exponents followed the same progression as our understanding of number (bin the beginning)