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It is fun to notice that our understanding of exponents followed the same progression as our understanding of number in the beginning