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 $\begin{aligned} x = log_b(y) & \Leftrightarrow \quad y = b^x \\ \text{Note: Domain of } log_b = \text{Range of } b^x = (0, \infty) \end{aligned}$