

Logarithmic Functions

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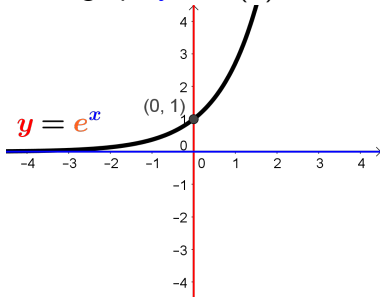
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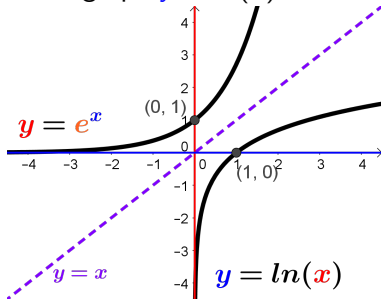
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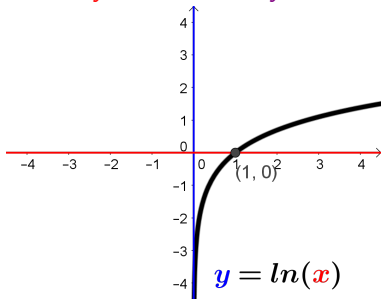
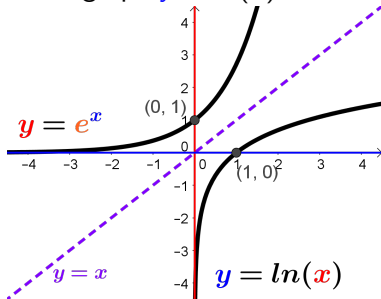
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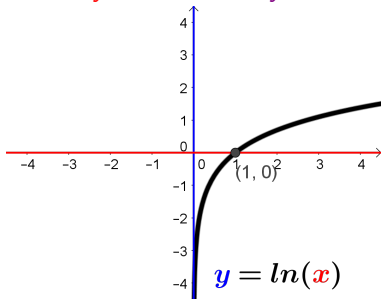
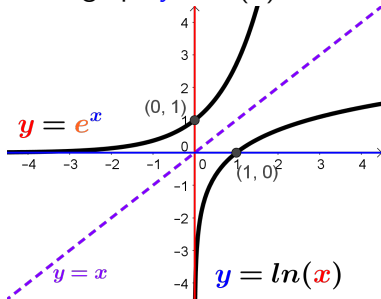
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Notice that the y -int at $(0, 1)$ reflects to the x -int at $(1, 0)$

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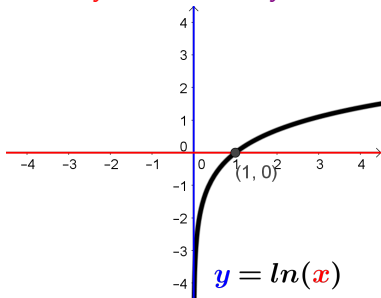
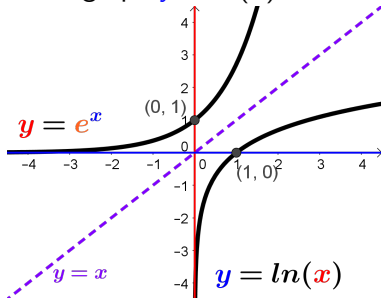
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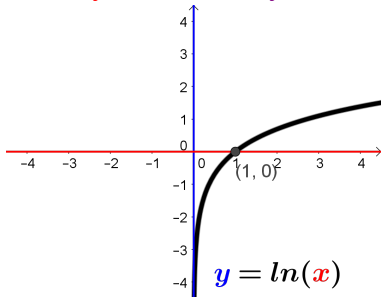
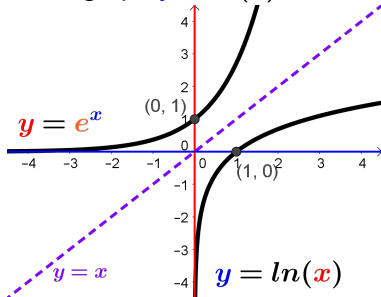
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The horiz. asymptote at $x = 0$ reflects to the vert. asymptote at $y = 0$