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We want to know the amount of time the money will be in the bank.

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▶ We saw that the amount of money when compounded continuously is given by:

$$P(t) = P_0 e^{rt}$$

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We're stuck! We need an inverse for exponentials to figure this out!